Using the distance based definition of a hyperbola,	find the equation of the hyperbola with foci $(0, \pm 12)$
such that the distances from any point on the hyperbola	a to the foci differ by 12.

SCORE: /10 PTS

Do NOT solve this problem using symbols in place of the numbers given.

$$\left| \sqrt{x^2 + (y+12)^2} - \sqrt{x^2 + (y-12)^2} \right| = 12$$

IF YOU FORGOT ± SEE ALTERNATE SOLUTION IF ORDER

$$\left| \sqrt{x^2 + (y+12)^2} - \sqrt{x^2 + (y-12)^2} \right| = 12$$

$$\sqrt{x^2 + (y+12)^2} - \sqrt{x^2 + (y-12)^2} = \pm 12$$

OF SUBTRACTION WAS REVERSED

$$\sqrt{x^2 + (y+12)^2} = \pm 12 + \sqrt{x^2 + (y-12)^2}$$

$$48y - 144 = \pm 24\sqrt{x^2 + y^2 - 24y + 144}$$

$$2y - 6 = \pm \sqrt{x^2 + y^2 - 24y + 144}$$

$$4y^2 - 24y + 36 = x^2 + y^2 - 24y + 144$$

$$4y^2 - 24y + 36 = x^2 + y^2 - 24y + 144$$

$$3y^2 - x^2 = 108$$

$$\frac{y^2}{36} - \frac{x^2}{108} = 1$$

Convert the rectangular equation y = 5x - 3 to polar form. Write r as function of θ , and simplify your answer. SCORE: _____/4 PTS

$$r\sin\theta = 5r\cos\theta - 3$$

$$r\sin\theta - 5r\cos\theta = -3$$

$$r(\sin\theta - 5\cos\theta) = -3$$

$$r(\sin\theta - 5\cos\theta) = -3$$

$$r = \frac{-3}{\sin \theta - 5\cos \theta} = \frac{3}{5\cos \theta - \sin \theta}$$

Fill	in	the	h	lan	ks

SCORE: /7 PTS

A house has an exposed (straight) beam 25 feet above and parallel to the floor. Two small lamps hang from the ceiling. [a]

There is an arch such that the total distance from one lamp to any point on the arch to the other lamp is exactly 18 feet.

The shape of the graph of the equation $4x^2 + 2x - 3y^2 - 3y - 1 = 0$ is a/an Type 30 LA [6]

The shape of the graph of the equation $3x^2 - 2x + 3y^2 - 3y - 1 = 0$ is a/an [c]

The polar co-ordinates $(-5, \frac{3\pi}{7})$ refer to the same point as the polar co-ordinates $(5, \frac{1077}{7})$. (Your answer must be **positive**.) [d]

The polar co-ordinates $(5, \frac{3\pi}{7})$ refer to the same point as the polar co-ordinates $(5, \frac{177}{7})$. (Your answer must be <u>negative</u>.) [e]

The point with polar co-ordinates $(-5, -\frac{4\pi}{3})$ lies in quadrant. [f]

Convert the polar equation $r^2 = \sin 2\theta$ to rectangular form.

SCORE: ____/4 PTS

Simplify your answer so that there are no radicals, complex fractions, fractional exponents nor negative exponents.

$$r^2 = 2\sin\theta\cos\theta$$

$$r^2 = 2\left(\frac{y}{r}\right)\left(\frac{x}{r}\right)$$
 OF

 $\mathbf{OR} \quad (r^2)r^2 = 2(r\sin\theta)(r\cos\theta)$



$$(x^{2} + y^{2})^{2} = 2xy$$

Find the foci, and equations of the asymptotes of the hyperbola $x^2 - 3y^2 - 4x - 18y - 17 = 0$.

SCORE: ____/5 PTS

$$(x^{2} - 4x) - 3(y^{2} + 6y) = 17$$
$$(x^{2} - 4x + 4) - 3(y^{2} + 6y + 9) = 17 + 4$$

$$(x^{2}-4x)-3(y^{2}+6y)=17$$

$$(x^{2}-4x+4)-3(y^{2}+6y+9)=17+4-27$$

$$(x-2)^{2}-3(y+3)^{2}=-6$$

$$\frac{(y+3)^{2}}{2}-\frac{(x-2)^{2}}{6}=1$$

$$\frac{(y+3)^2}{2} - \frac{(x-2)^2}{6} = 1$$

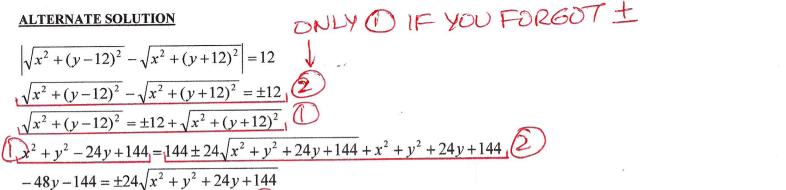
$$c^2 = 2 + 6 = 8 \quad \Rightarrow \quad c = 2\sqrt{2}$$

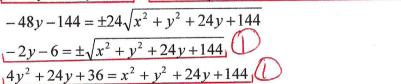
slopes of asymptotes
$$=\pm\sqrt{\frac{2}{6}}=\pm\sqrt{\frac{1}{3}}=\pm\frac{\sqrt{3}}{3}$$

FOCI:

$$(2, -3 \pm 2\sqrt{2})$$

ASYMPTOTES:
$$y+3 = \pm \frac{\sqrt{3}}{3}(x-2)$$





 $3y^2 - x^2 = 108$